

Magnetska rezonancija

1. Čestice u magnetnom polju
2. Eksperimentalne tehnike
3. NMR spektroskopija

Čestice u magnetskom polju

Čestice koje posjeduju spinsku kutnu količnu gibanja orijentiraju se u magnetskom polju.

Elektron e , e^-

Kvantni broj elektronskog
spina s

$$s = \frac{1}{2}$$

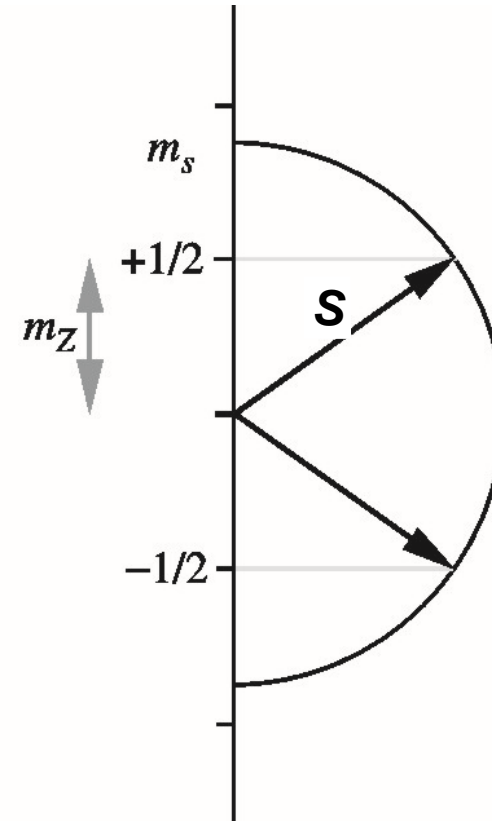
$$|\mathbf{S}| = \sqrt{s(s+1)} \hbar = \sqrt{3/4} \hbar$$

z-komponenta elektronskog spina
magnetski kvantni broj spina

m_s

$$m_s \rightarrow +\frac{1}{2}, -\frac{1}{2}$$

$$S_z = m_s \hbar = \pm \frac{1}{2} \hbar$$



Proton p, p⁺, ¹H⁺

$$|\mathbf{I}| = \sqrt{I(I+1)} \hbar = \sqrt{3/4} \hbar$$

$$I_z = m_I \hbar = \pm \frac{1}{2} \hbar$$

Jezgre

$$|\mathbf{I}| = \sqrt{I(I+1)} \hbar$$

$$I_z = m_I \hbar$$

Kvantni broj nuklearnog
spina I

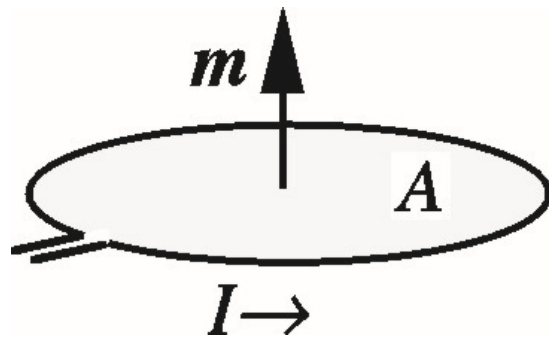
$$I \rightarrow 0, \frac{1}{2}, 1, \frac{3}{2}, \dots$$

Z-komponenta nuklearnog spina
magnetski kvantni broj nuklearnog spina m_I

$$m_I \rightarrow I, I - 1, \dots, 0, \dots - I + 1, -I$$

$$m_I \rightarrow I, I - 1, \dots, \frac{1}{2}, -\frac{1}{2}, \dots - I$$

Magnetski moment strujne petlje

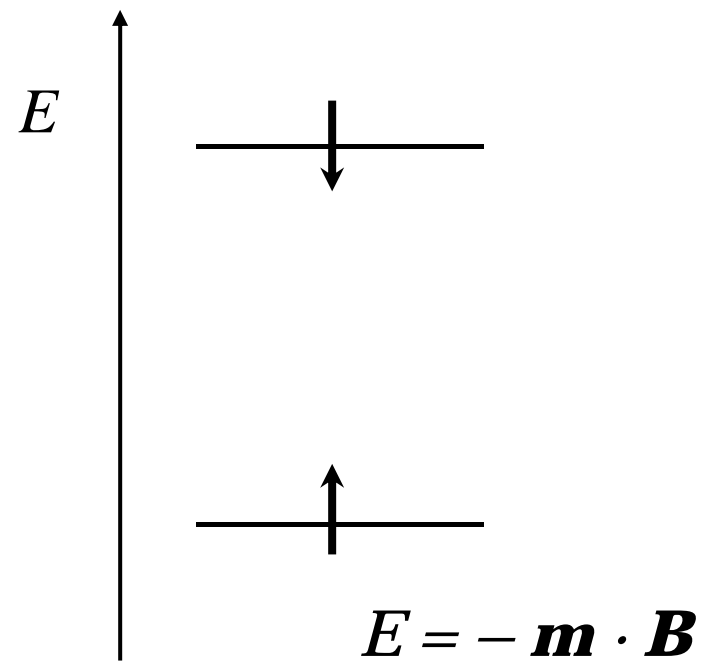
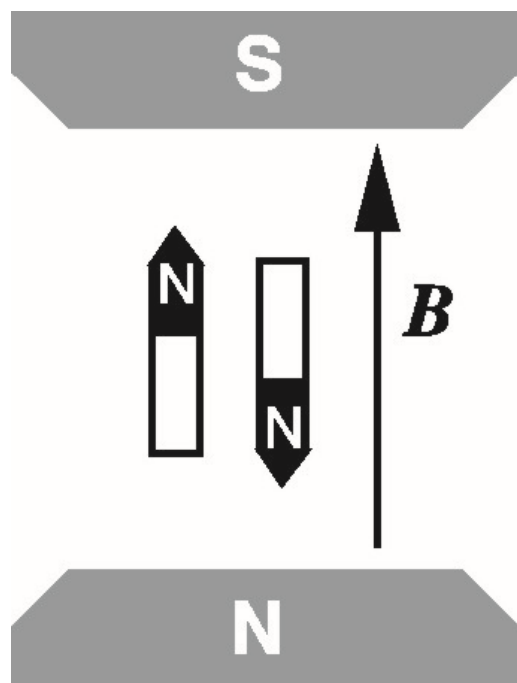


$$\mathbf{m} = I \mathbf{A}$$

$$|\mathbf{m}| = \frac{Qv}{2r\pi} r^2 \pi = \frac{Qvr}{2}$$

$$L = mvr$$

$$\gamma = \frac{|\mathbf{m}|}{|\mathbf{L}|} = \frac{|Q|}{2m} = \left(\frac{g e}{2m} \right)$$



Elektron

Magnetski moment elektrona

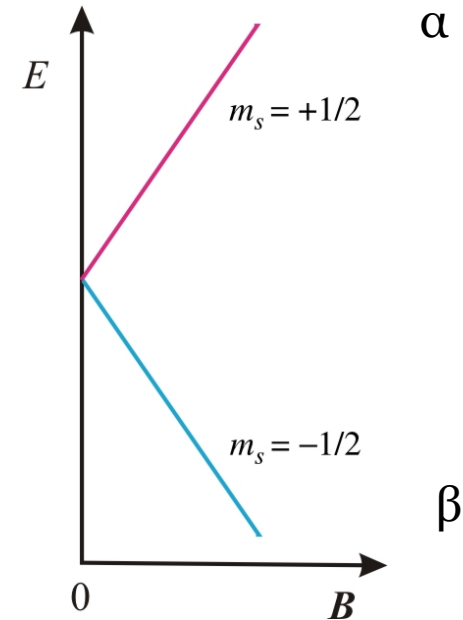
$$\mathbf{m} = g \frac{-e\hbar}{2m_e} \sqrt{s(s+1)}$$

$$\mathbf{m} = -g \mu_B \sqrt{s(s+1)}$$

Bohrov magneton $\mu_B = \frac{e\hbar}{2m_e} \approx 9,273 \times 10^{-24} \text{ J T}^{-1}$

Komponenta magnetskog momenta elektrona duž osi Z

$$m_Z = -g \mu_B m_s$$



Energija interakcije magnetskog momenta m s magnetskom indukcijom B

$$\mathbf{E} = -\mathbf{m} \cdot \mathbf{B}$$

$$E = g \mu_B m_s B$$

Jezgra

Magnetski moment jezgre

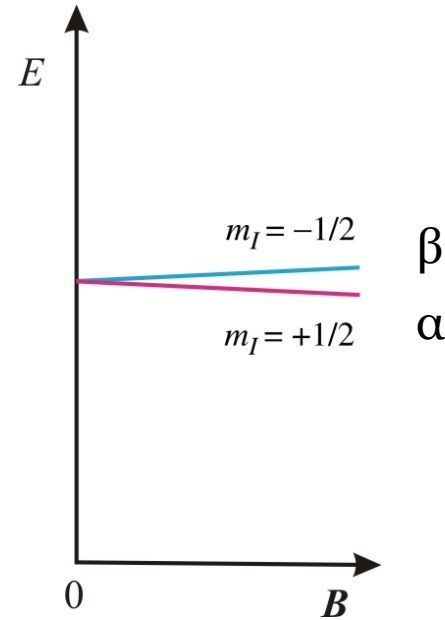
$$\mathbf{m} = g \frac{e\hbar}{2m_p} \sqrt{I(I+1)}$$

$$\mathbf{m} = g \mu_N \sqrt{I(I+1)}$$

Nuklearni magneton $\mu_N = \frac{e\hbar}{2m_p} \approx 5,051 \times 10^{-27} \text{ J T}^{-1}$

Komponenta magnetskog momenta jezgre duž osi Z

$$m_Z = g \mu_N m_I$$

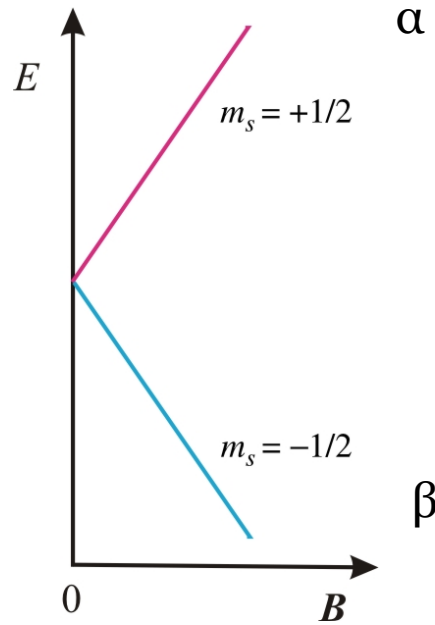


Energija interakcije magnetskog momenta m s magnetskom indukcijom B (jezgra s $I = 1/2$)

$$\mathbf{E} = -\mathbf{m} \cdot \mathbf{B}$$

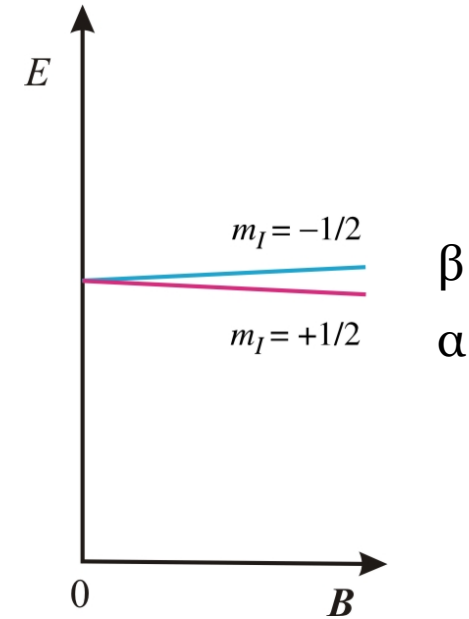
$$E = -g \mu_N m_I B$$

Elektron



$$E = -g \mu_B m_I B$$

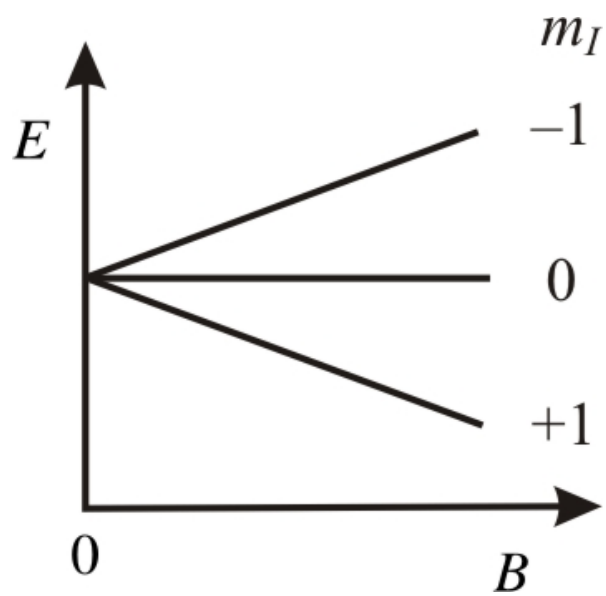
Jezgra ($m_I = \pm \frac{1}{2}$)



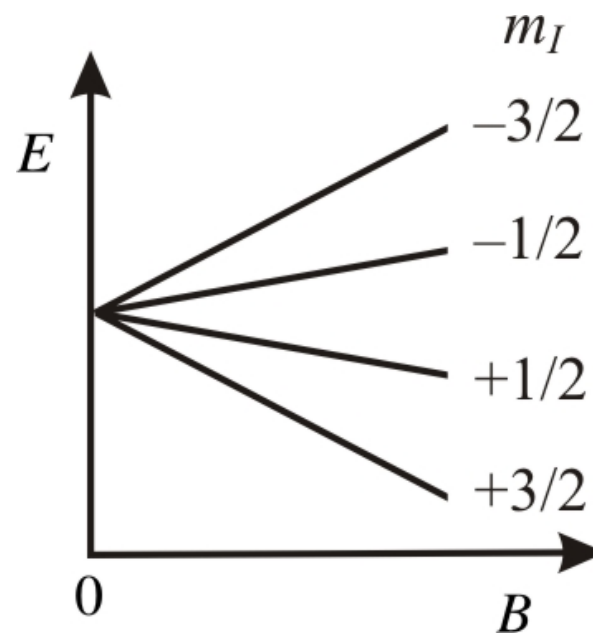
$$E = -g \mu_N m_I B$$

$$\frac{\mu_B}{\mu_N} = \frac{m_p}{m_e}$$

$$I = 1$$



$$I = 3/2$$



$$E = -g \mu_N m_I B$$

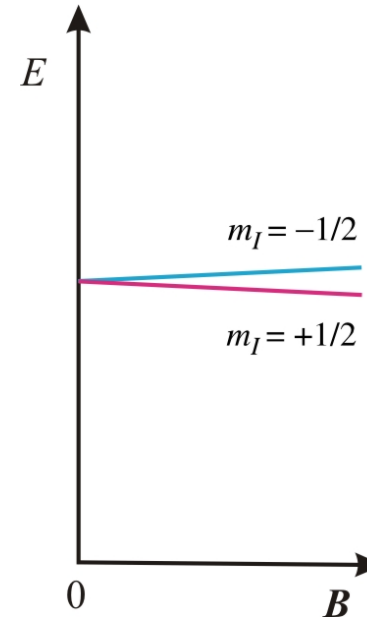
Frekvencija rezonancije

Jezgra ($m_I = \pm \frac{1}{2}$)

$$\nu = \frac{\Delta E}{h}$$

$$\Delta m_I = \pm 1$$

$$\Delta E = E(m_I - 1) - E(m_I) = g \mu_N B = h \nu_L$$



Popunjenost energetske razine

- Boltzmanova raspodjela

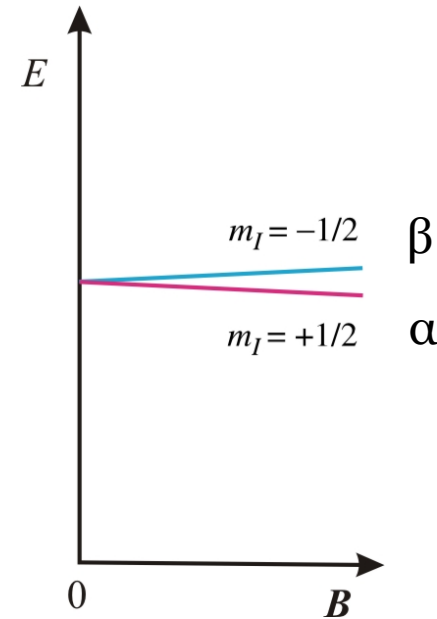
$$\frac{N_{\beta}}{N_{\alpha}} = \exp\left(-\frac{(E_{\beta} - E_{\alpha})}{k_B T}\right)$$

$$E_{\beta} - E_{\alpha} > 0$$

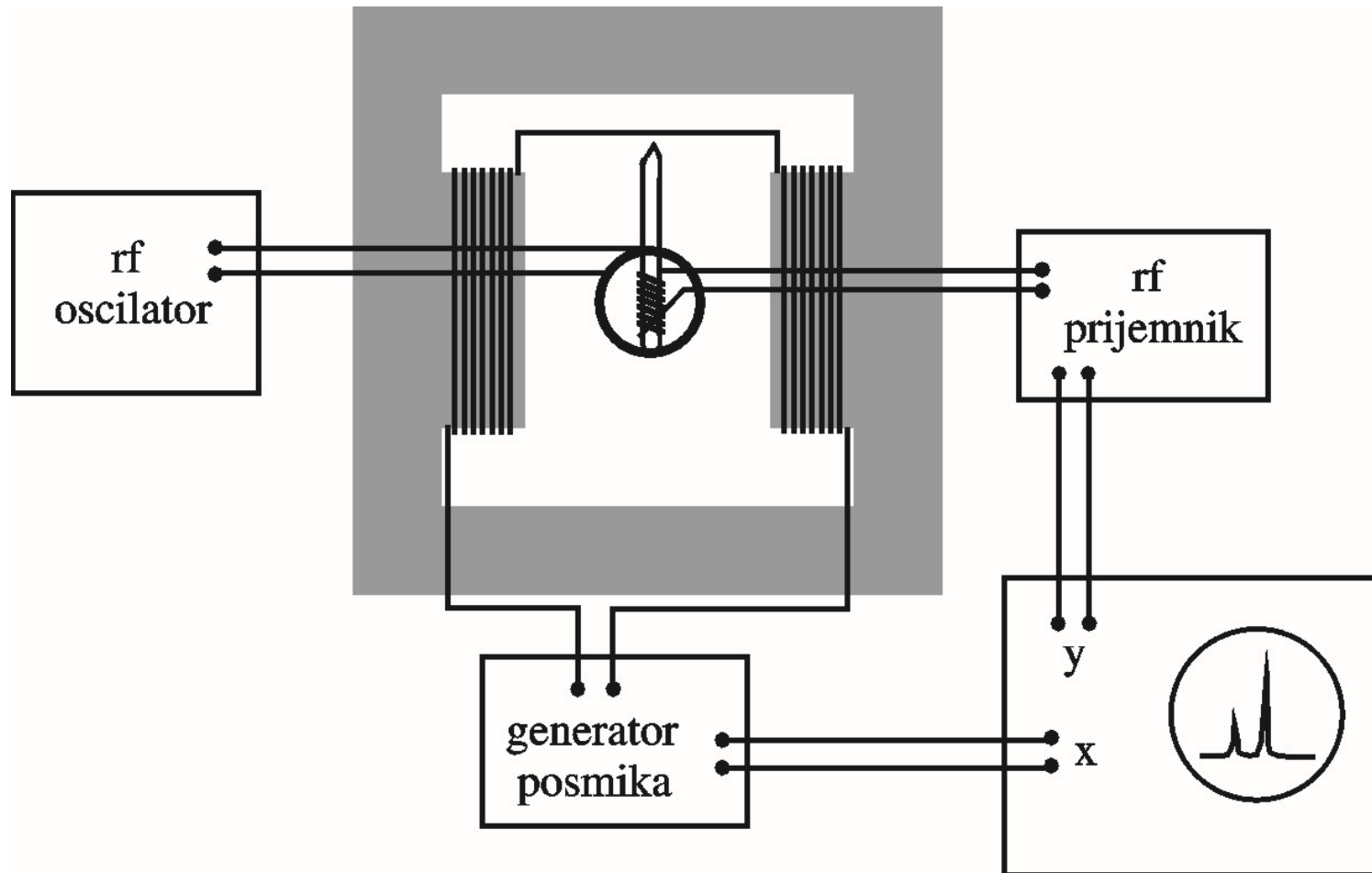
$$\frac{N_{\beta}}{N_{\alpha}} < 1$$

$$N_{\beta} < N_{\alpha}$$

Jezgra ($m_I = \pm \frac{1}{2}$)

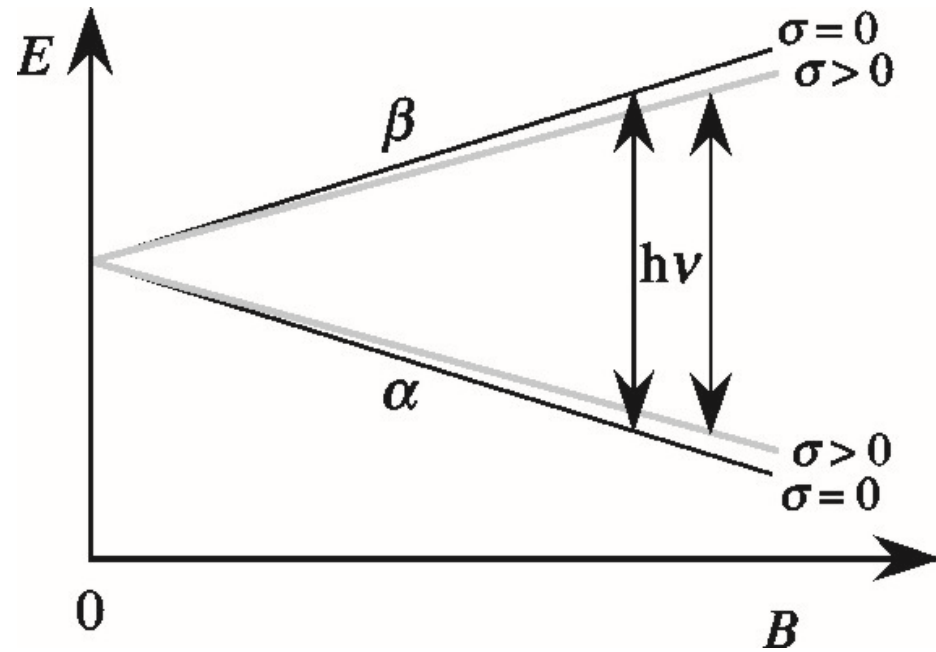
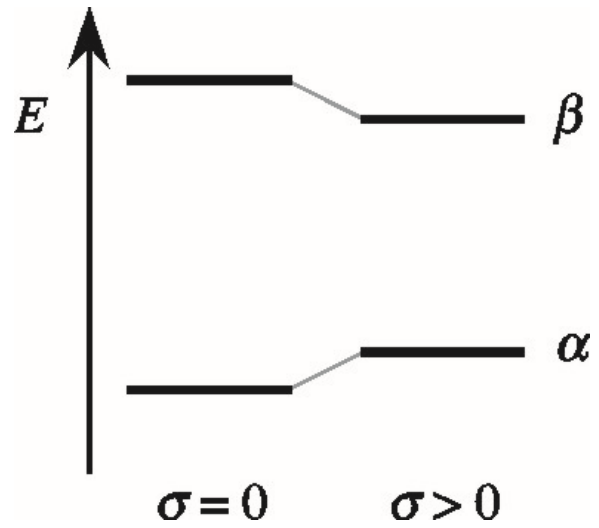


Shema NMR spektrometra

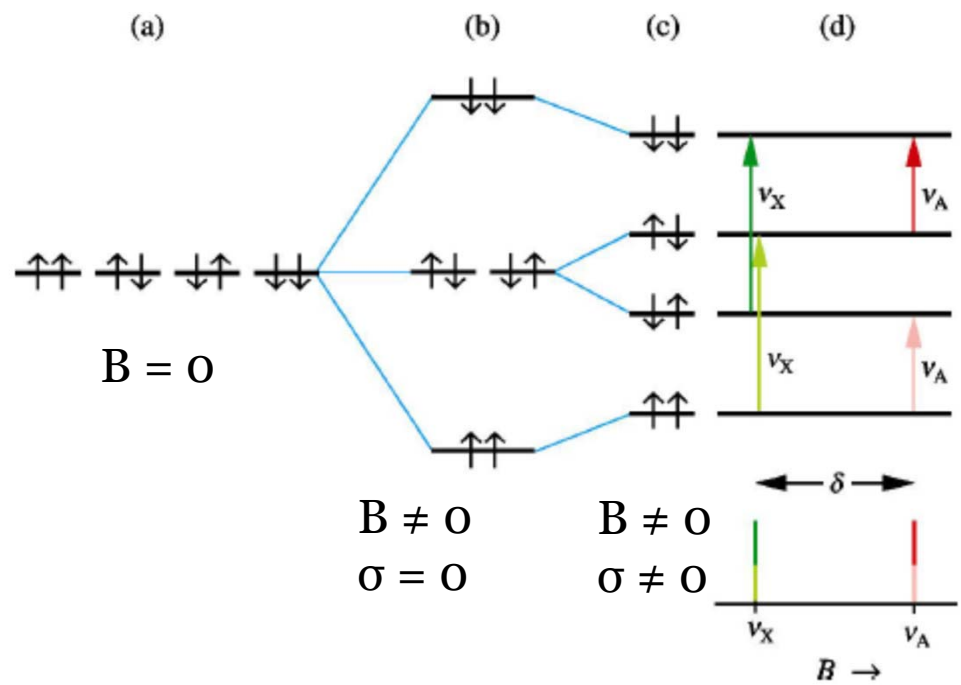


Kemijski pomak

$$B = B_0(1 - \sigma)$$



1) RAZINE SPINSKIH STANJA DVAJU PROTONA



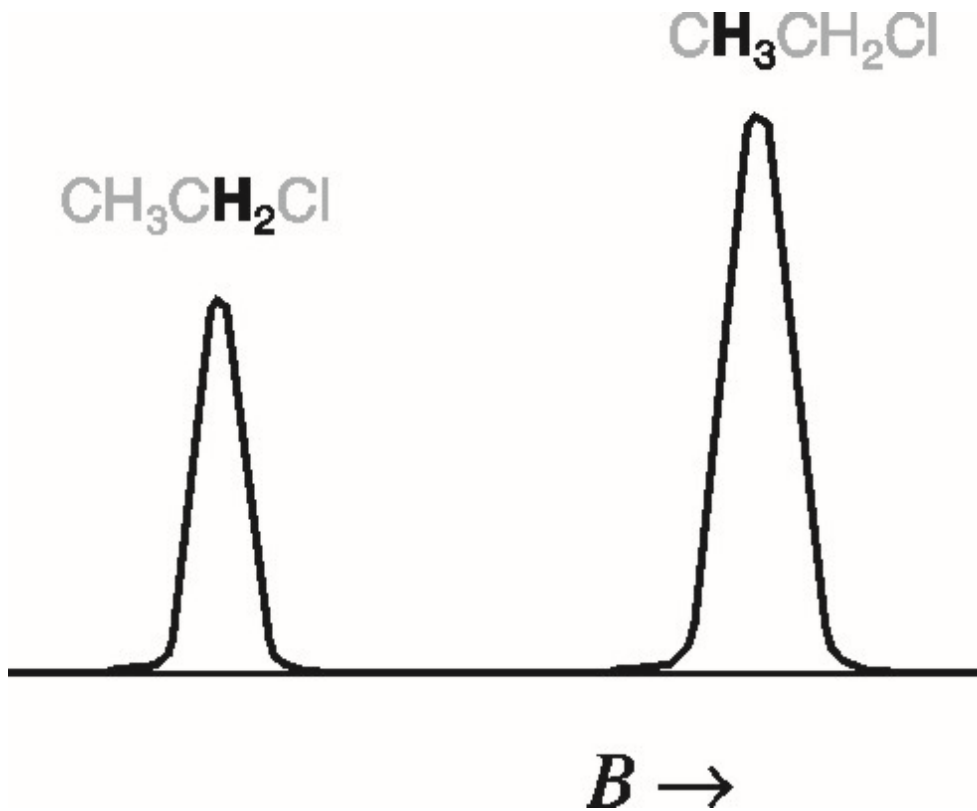
PRIJELAZI

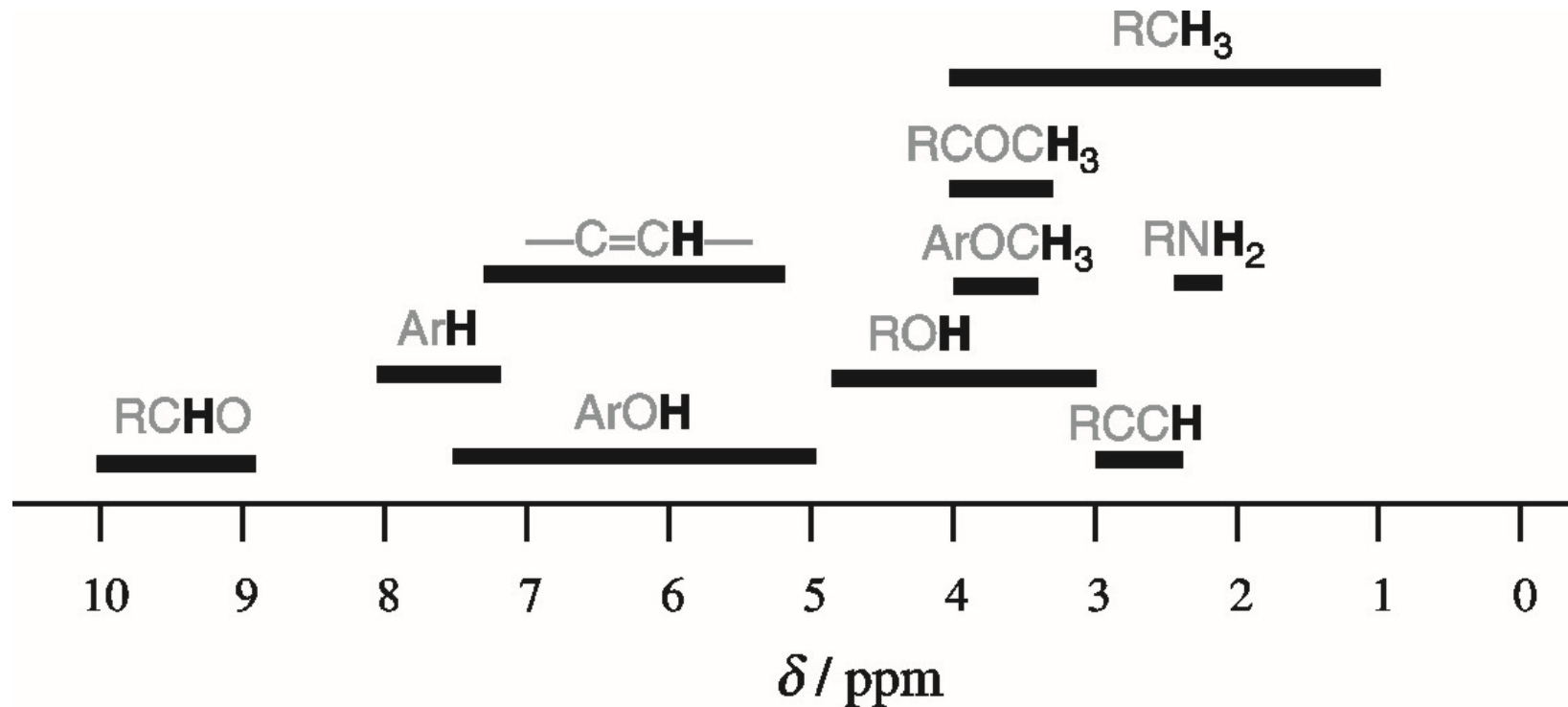
SPEKTAR

$$\delta_X = (\sigma_{\text{ref}} - \sigma_X) \times 10^6 \text{ ppm}$$

$$\delta_X \approx \frac{B_i - B_{\text{ref}}}{B_{\text{ref}}} \times 10^6 \text{ ppm} = \frac{B_0(1 - \sigma_X) - B_0(1 - \sigma_{\text{ref}})}{B_0(1 - \sigma_{\text{ref}})} \times 10^6 \text{ ppm}$$

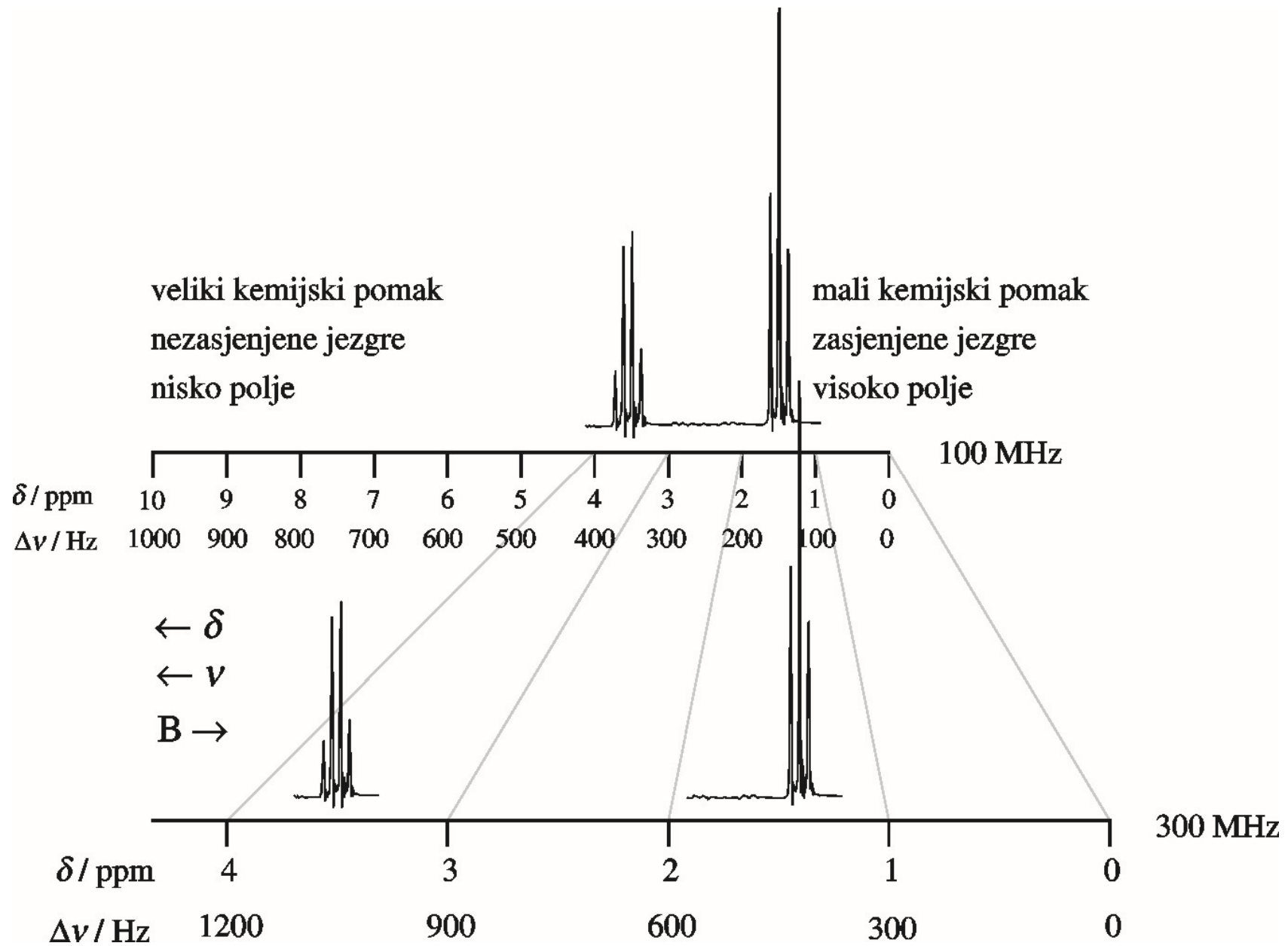
$$\delta_X \approx \frac{\Delta\nu}{\nu_{\text{ref}}} \times 10^6 \text{ ppm}$$





Zasjenjenje:

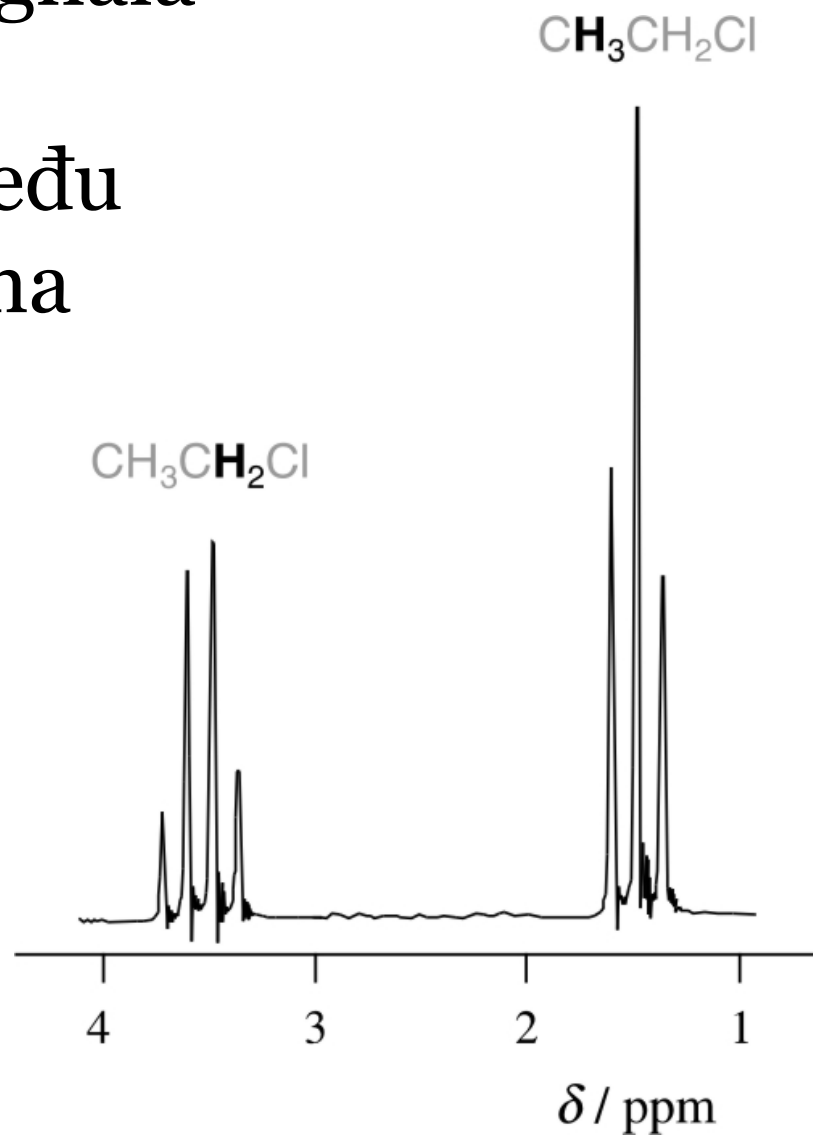
- lokalni doprinos (elektroni)
- doprinosi susjednih i daljnjih atoma
- doprinos otapala

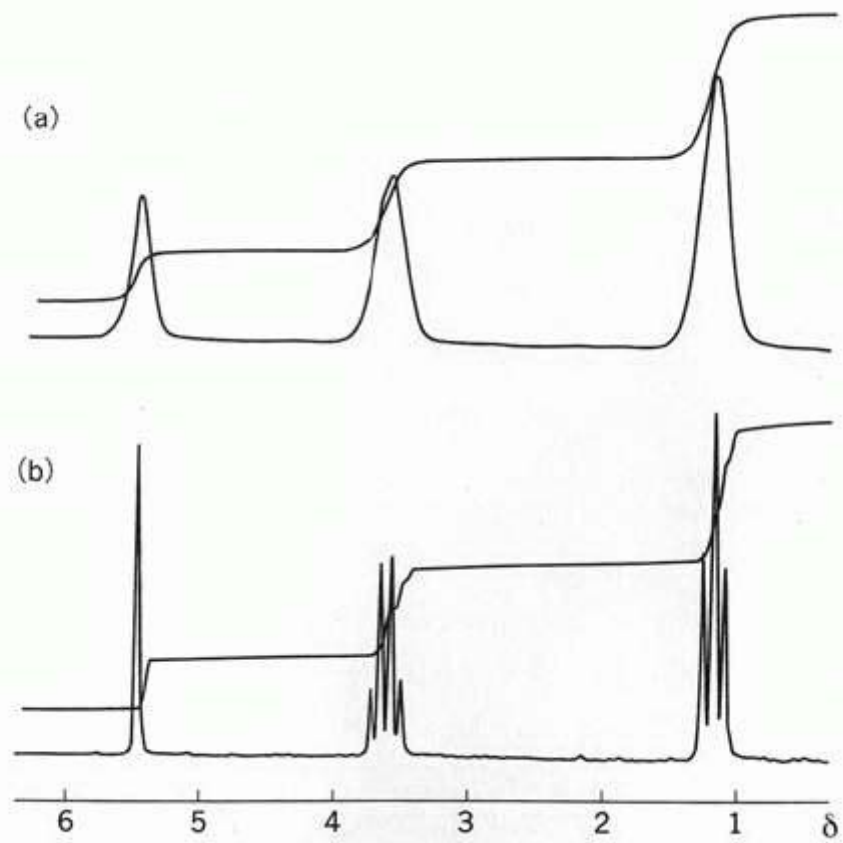


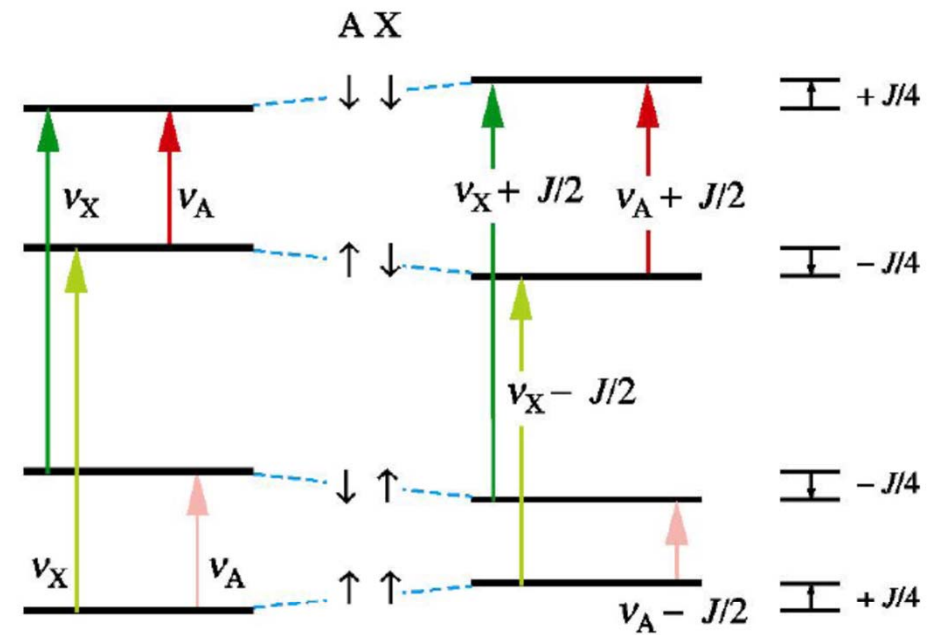
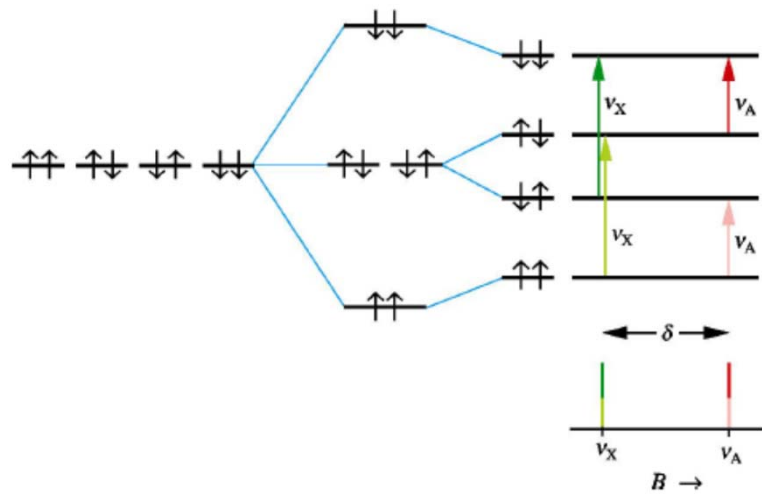
Cijepanje signala

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Sprega među spinovima

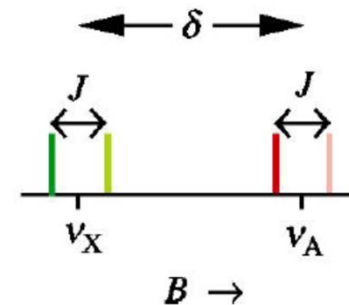
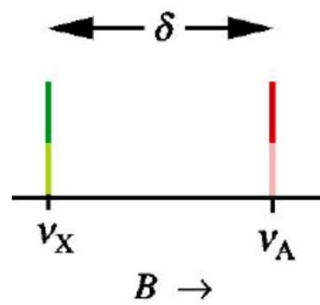






$$J_{AX} = 0$$

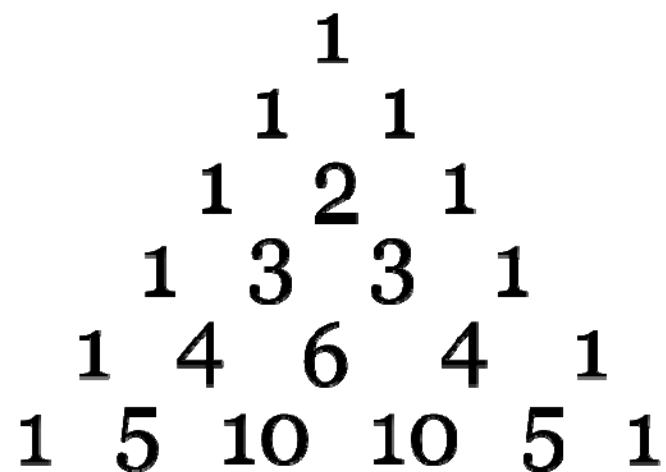
$$J_{AX} > 0$$

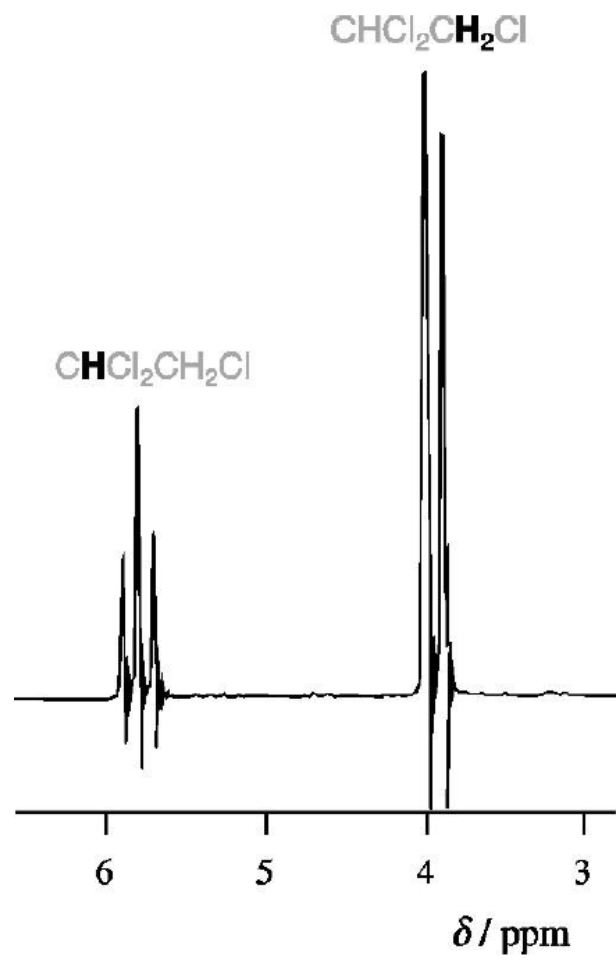
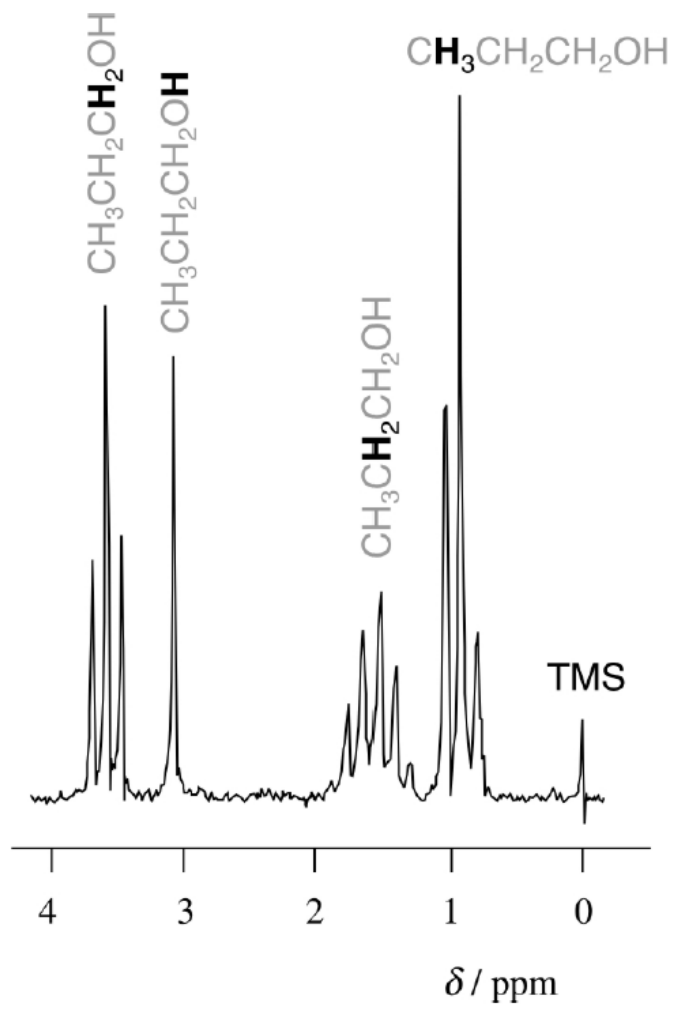


Cijepanje linija - spin-spin sprega

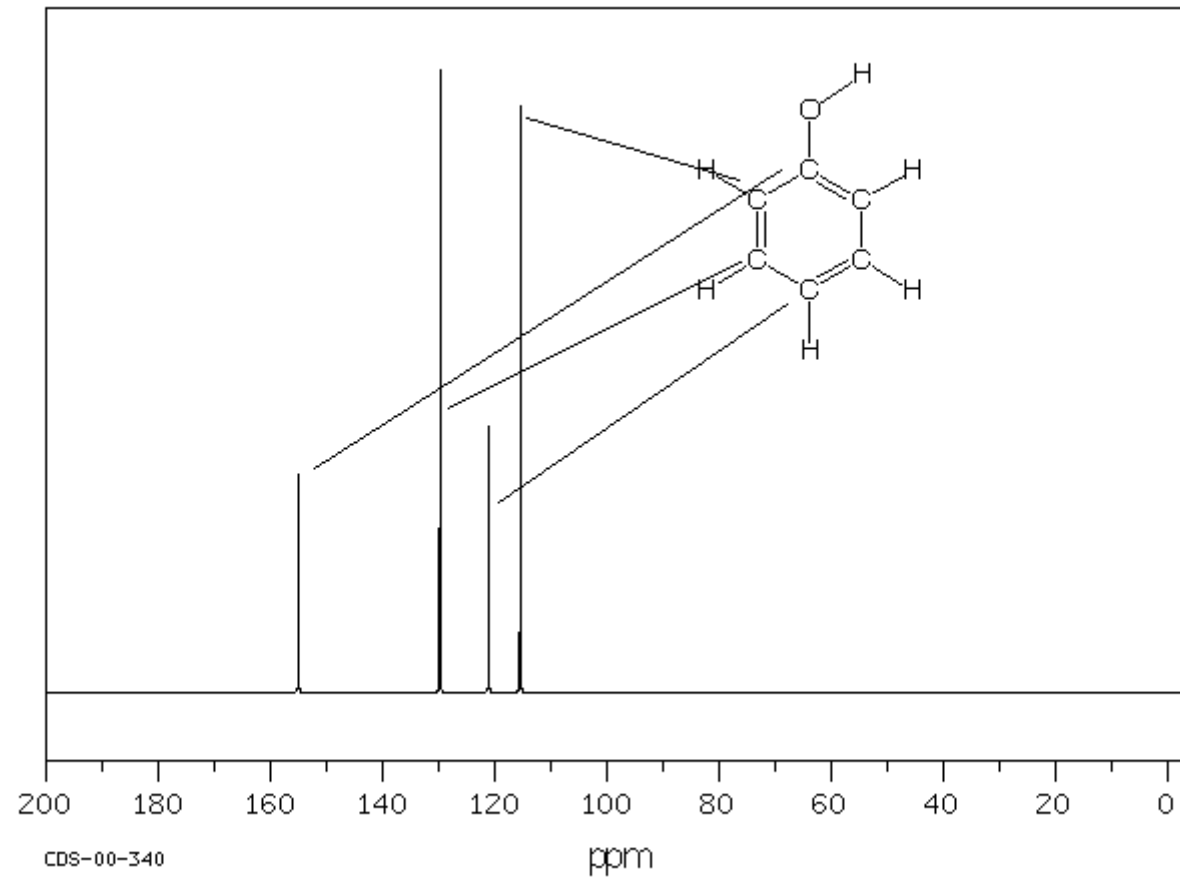
N susjednih protona → N+1 LINIJA

Intenziteti: Pascalov trokut





^{13}C - NMR



MAGNETSKA REZONANCIJA

1. Koje jezgre imaju magnetski moment?
2. Koliko je mogućih orijentacija magnetskog momenta ako je nuklearni spinski kvantni broj $9/2$ (^{209}Bi)?
3. Koliko je mogućih orijentacija magnetskog momenta ako je nuklearni spinski kvantni broj 8 (^{180}Ta)?
4. Nabrojite neke jezgre s $I = 0$.
5. Nabrojite neke jezgre s $I = 1/2$.
6. Koja je čestica jači magnet: elektron ili proton?
7. Kakva je energija interakcije magnetskog momenta s magnetskim poljem?
8. Što je Larmorova frekvencija?
9. Kako ovisi separacija energijskih razina o magnetskoj indukciji primjenjenog magneta?
10. Što inducira prijelaze među nuklearnim spinskim razinama?
11. Koje se zračenje primjenjuje u NMR?

NMR

1. Kojeg su reda veličine magnetske indukcije kod NMR-spektrometara?
2. Što je uzrok kemijskom pomaku?
3. Što iskazuje konstanta zasjenjenja?
4. Zašto elektroni slabe utjecaj vanjskog polja na jezgre?
5. Kakav efekt na spektar ima zasjenjenje jezgara?
7. Zašto su kemijski pomaci kod ugljika znatno veći nego kod protona?
8. Prikažite energijske razine i prijelaze za dva protona u različitim kemijskim sredinama.
9. Koji utjecaji pridonose kemijskom pomaku?
10. Kako susjedni atomi utječu na kemijski pomak?
Objasnite sprezanja među spinovima vodikovih atoma susjednih funkcionalnih skupina?
12. Objasnite nastajanje tripleta linija.
13. Objasnite nastajanje kvadrupleta linija.