

# Velocity - Range - Wavelength relationships

- Fundamental sampling theorem states that to measure a frequency of  $f$ , it is necessary to sample at least at  $(2f)$

$$\text{Sampling rate} = \text{PRF} \Rightarrow 2f = \text{PRF}$$

- Doppler theorem states that velocity is related to the frequency shift  $f$  by

$$V = - \frac{f \lambda}{2}$$

$$\left\{ \begin{aligned} \delta V_{\text{rain}} &= -\delta f \lambda \\ \delta V_{\text{cloud}} &= -\delta f \lambda \end{aligned} \right.$$

- Nyquist interval

$$V_{\text{max}} = \pm \frac{(\text{PRF}) \lambda}{4} = \frac{f \lambda}{2}$$

IF PRF  $10^3$  ... S-band (10cm)  $\Rightarrow \pm 25 \text{ m/s}$   
 X-band (3cm)  $\Rightarrow \pm 8 \text{ m/s}$  } UNAMBI  
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- Increasing PRF to extend  $V_{\text{max}}$  decreases  $R_{\text{max}}$

$$\frac{V_{\text{max}} R_{\text{max}}}{\frac{\text{PRF}}{2} \frac{c}{2 \cdot \text{PRF}}} = \pm \frac{\lambda c}{8} \quad \therefore \text{CONST.}$$

- Increasing  $\lambda \Rightarrow \sigma$  decreases ( $\sigma \propto \frac{1}{\lambda^4}$ )  $\Rightarrow \bar{P}_r$  decreases ( $\bar{P}_r \propto \sigma$ )

- S-band can generally detect rain but not cloud droplets  
 K-band will detect many cloud droplets even if they not are yielding precipitation