



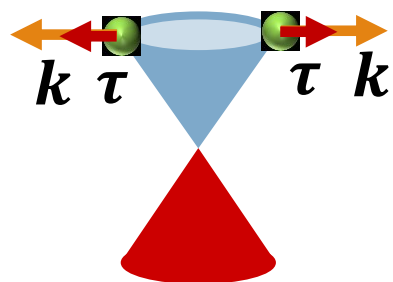
Evidence of 3D Dirac dispersion in PbSnSe by the de Haas - van Alphen oscillations

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GRAPHENE

$$\hat{H}_{2D} = \hbar v_F \boldsymbol{\tau} \cdot \mathbf{k}$$

- Lattice pseudospin
- Pseudospin – momentum locking - helicity



- 2D system
- Weak S-O interaction
- Lattice symmetry protection

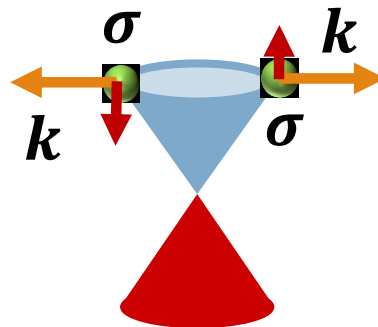
By Google 10⁷

VS

TOPOLOGICAL INSULATORS

$$\hat{H}_{2D} = \hbar v_F \boldsymbol{\sigma} \cdot \mathbf{k}$$

- Real spin
- Spin – momentum locking: $\mathbf{k} \perp \boldsymbol{\sigma}$ *in plane*



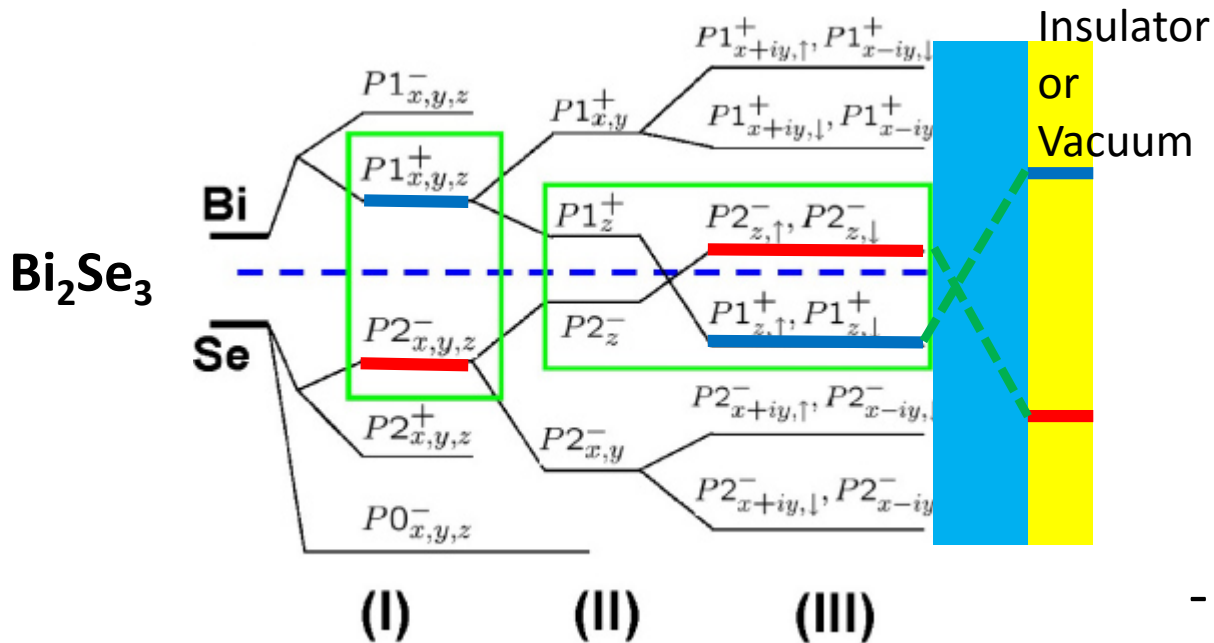
- 2D QSH
- 3D \mathbb{Z}_2 invariants
- Strong S-O interaction
- TRS protection

By Google 10⁵

What are Topological insulators

- ❖ Special materials with insulating bulk and conducting surface
- ❖ Origin of metallic surface lies special properties of bulk wave function

Bulk surface correspondence



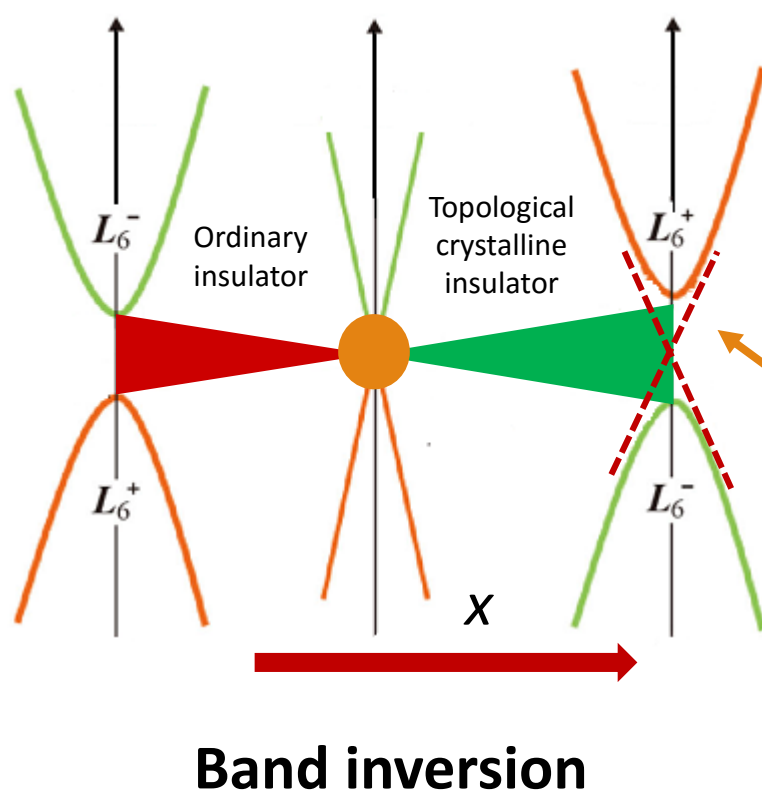
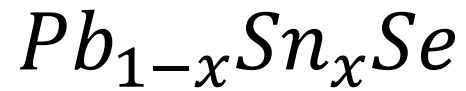
- ❖ Band inversion is curtail – NONTRIVIAL TOPOLOGY
- ❖ Dirac cones at TRS points
- ❖ Odd number of Dirac cones in the band gap

Interesting field for testing Elemental Particle Physics concepts

- Dirac, Weyl and Majorana fermion, magnetic monopoles and axion dynamics

PbSnSe and Topological Crystalline Insulators

❖ Topological Crystalline Insulators $TRS \leftrightarrow \text{Crystal Symmetry}$



For $x=0.17$ critical point

- band inversion point

I. Zeljkovic et al.

Nature Materials **14**, 318 (2015)

@ $x=0.17$

-Topological phase transition

- 3D Dirac dispersion?

3D Dirac semimetals

- 3D equivalent of graphene

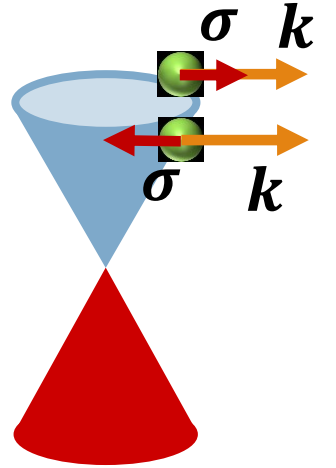
$$\hat{H}_{3D} = \hbar v_F \boldsymbol{\sigma} \cdot \mathbf{k}$$

$\sigma_x, \sigma_y, \sigma_z$ Spin Pauli matrix

k_x, k_y, k_z kristal momentum

- ❖ Robust to perturbation
- ❖ Dirac cone is spin degenerated
- ❖ Helicity

$$\chi = \frac{\boldsymbol{\sigma} \cdot \mathbf{k}}{\sigma k}$$



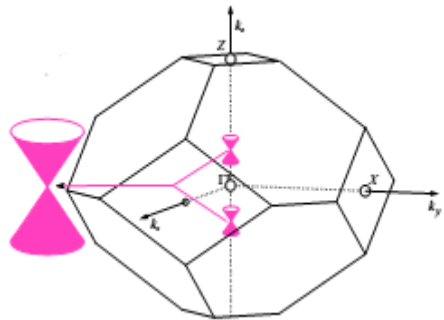
- ❖ 3D Dirac semimetals have nontrivial topology – due to band inversion- strong S-O interaction

- ❖ Band gap is not open to crate Topological Insulator

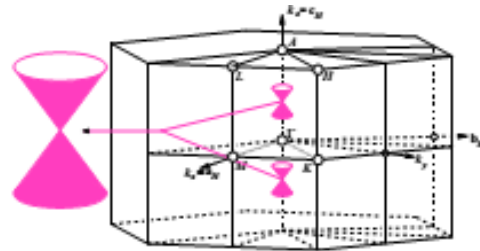
Intrinsic 3D Dirac semimetal

- Crystal symmetry protection from gap opening

Cd_3As_2 , Na_3Bi , BaAgBi



Cd_3As_2



Na_3Bi

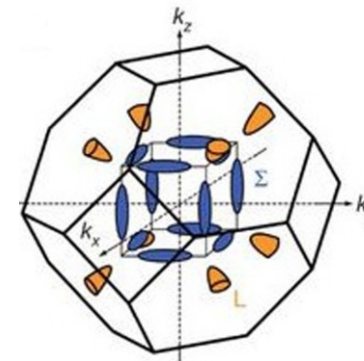
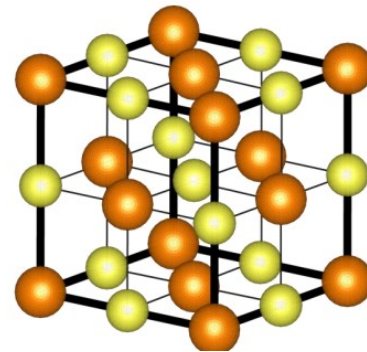
Q. D Gipson et al. [arXiv:1411.0005](https://arxiv.org/abs/1411.0005)

- High mobility $10^7 \text{ cm}^2/\text{Vs}$
- Very strong MR
- Giant diamagnetism

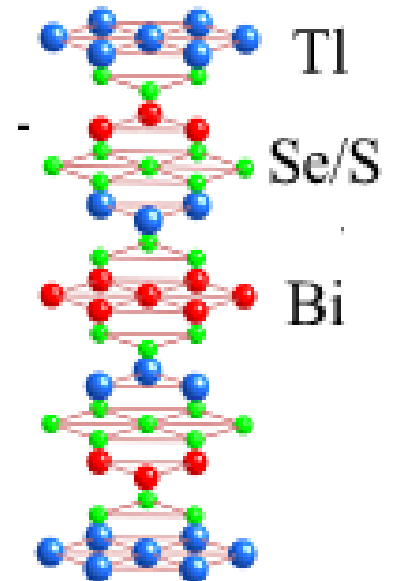
Accidental band touching

- Nontrivial topology
- CB and VB touching by composition tuning
- Always at Topological critical point

$\text{Pb}_{1-x}\text{Sn}_x\text{Se}$, $\text{Pb}_{1-x}\text{Sn}_x\text{Te}$



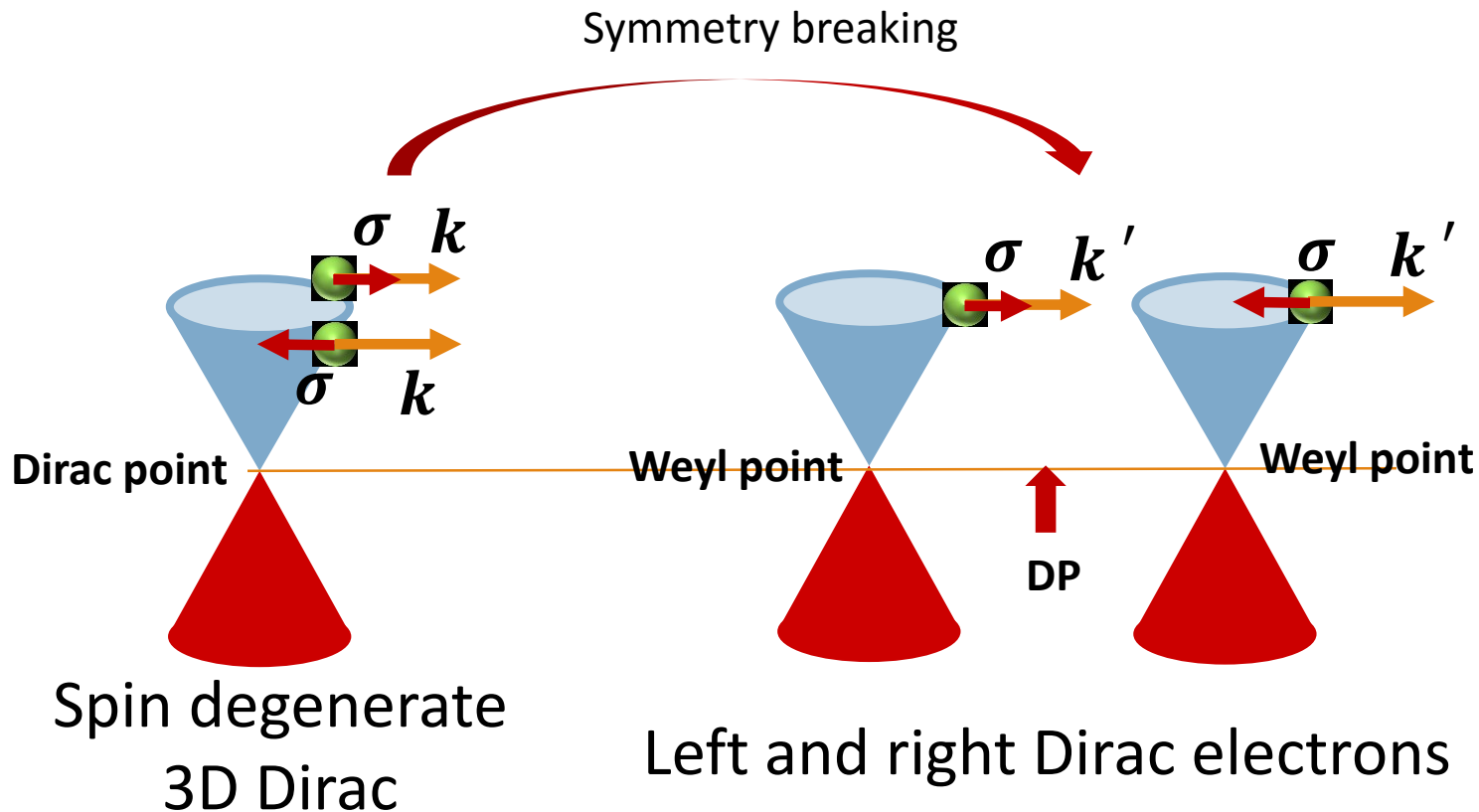
TlBiSse



Beyond 3D Dirac systems: Weyl semimetals

❖ New state of matter – Chiral Dirac particles

$$\hat{H}_{3D} = \pm \hbar v_F \boldsymbol{\sigma} \cdot \mathbf{k}'$$



Family of recently predicted WSM

TaAs, TaP, NbAs, NbP

arXiv: 1501.00755

How to get information on type dispersion by magnetic and transport measurements?

❖ Landau quantization and de Haas van Alphen oscillations (dHvA)

❖ Osanger's relation $A_k(\epsilon_k) = (n + \gamma)2\pi eB/\hbar$

❖ Berry phase $\phi_B = 2\pi \left(\frac{1}{2} - \gamma \right)$

Phase factor

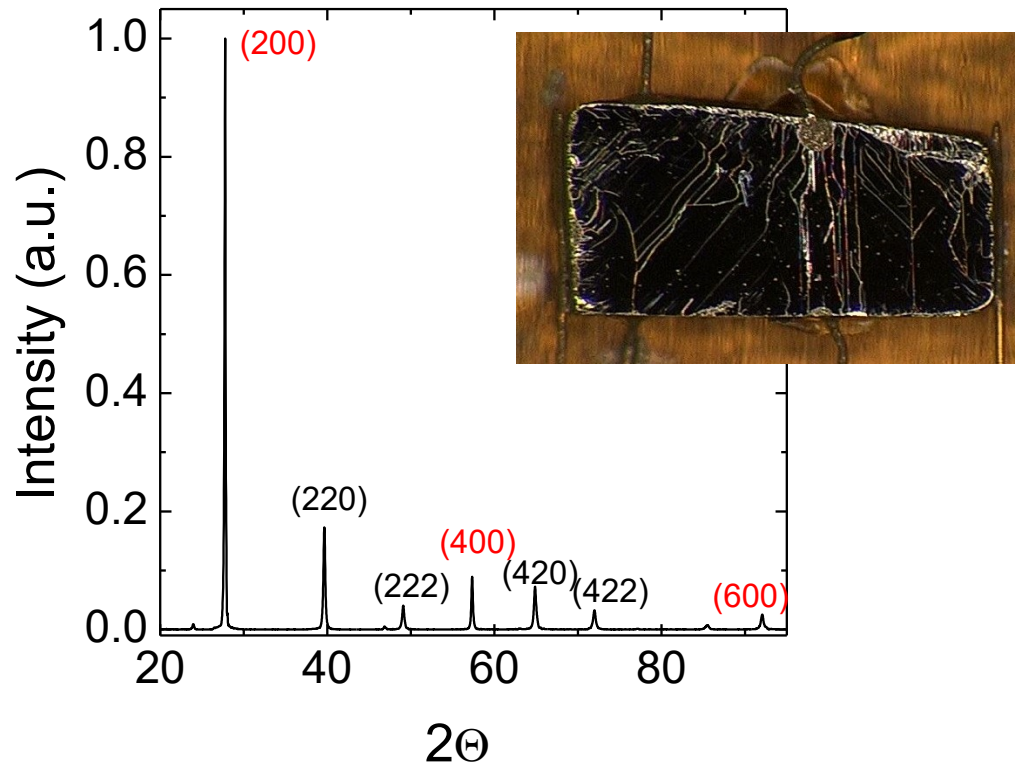
$$\phi(\gamma) = 2\pi \left(\frac{1}{4} \pm \frac{1}{4} - \gamma \pm \frac{1}{8} \right)$$

❖ dHvA $\Delta M \sim A(T, B) \sin\left(\frac{2\pi F}{B} + \phi(\gamma)\right)$

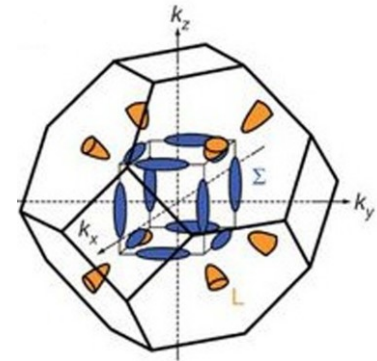
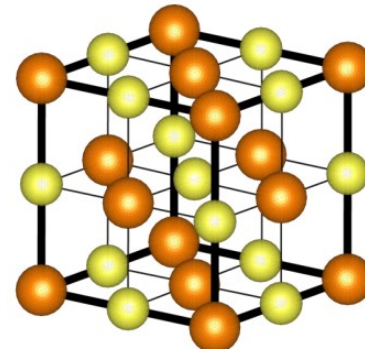
$\gamma = \frac{1}{2}$ Parabolic
 $\gamma = 0$ Linear

Sample information

❖ Sample: Monocrystal of $\text{Pb}_{0.83}\text{Sn}_{0.17}\text{Se}$ with reduced charge carriers $\sim 10^{17} \text{ cm}^{-3}$

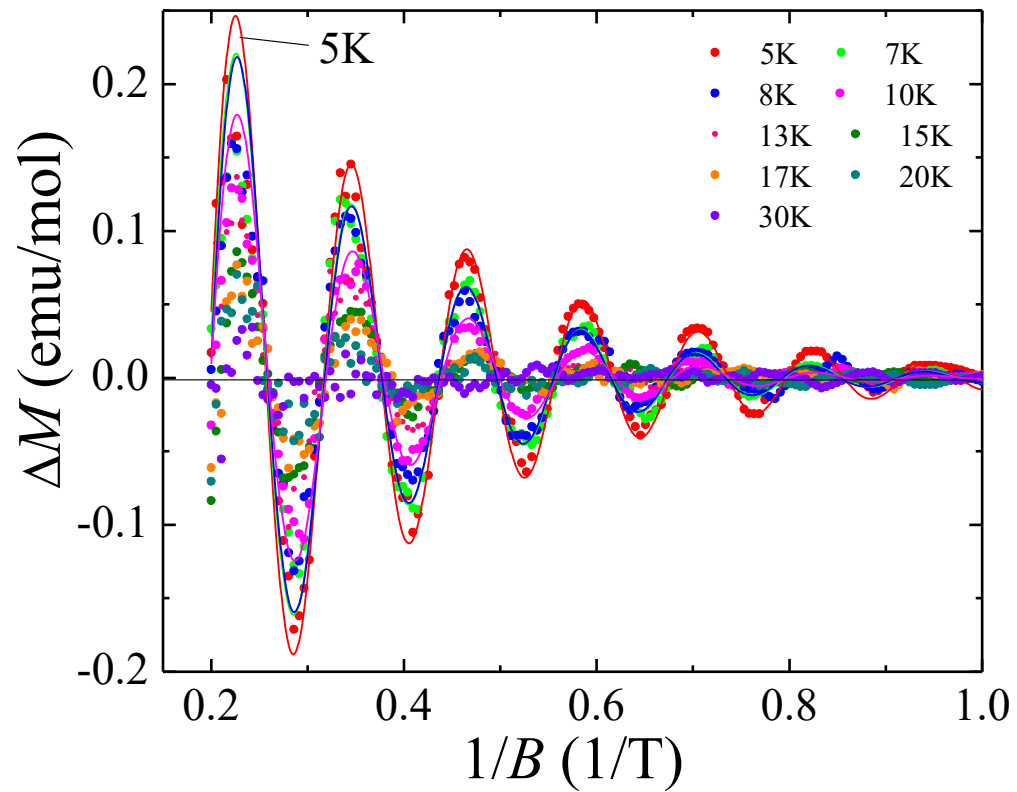


❖ Samples were grown by modified Bridgman method

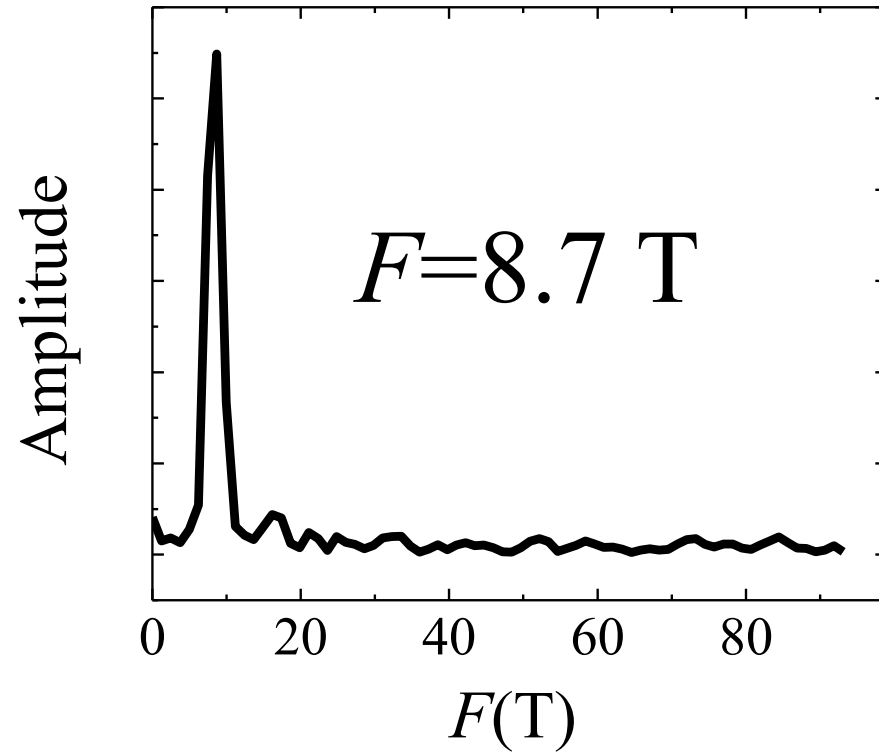


Solid solution with cubic structure

SQUID measurements of dHvA oscillations



dHvA oscillations

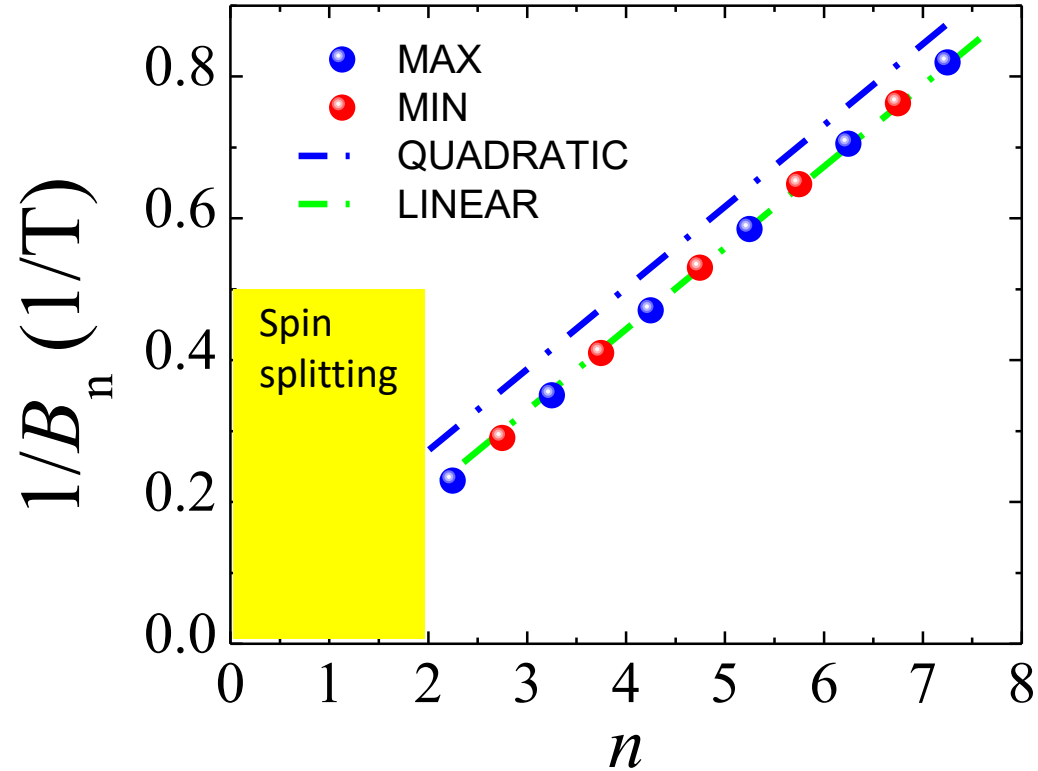


FFT of the oscillations

Phase determination

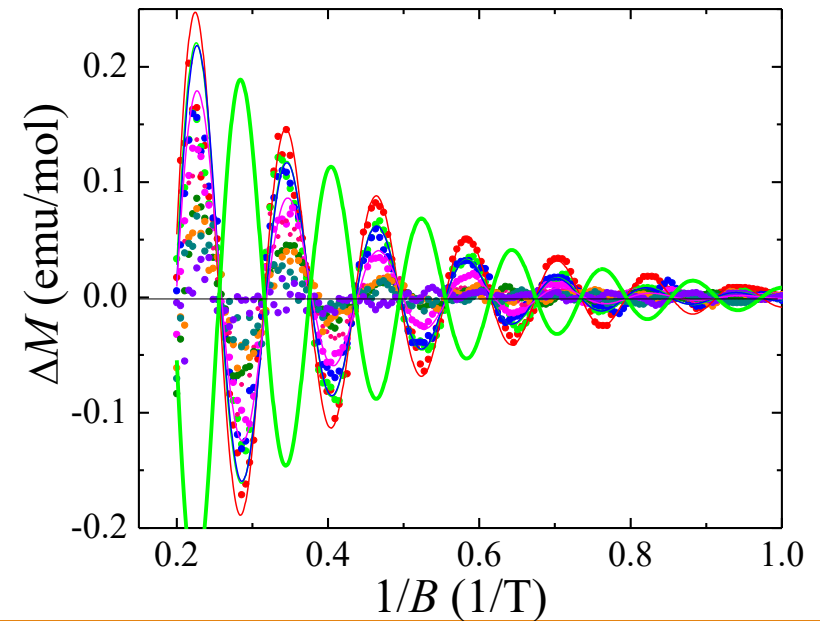
❖ Landau level indexing

$$\phi(\gamma) = 2\pi\left(\frac{1}{4} \pm \frac{1}{4} - \gamma \pm \frac{1}{8}\right)$$

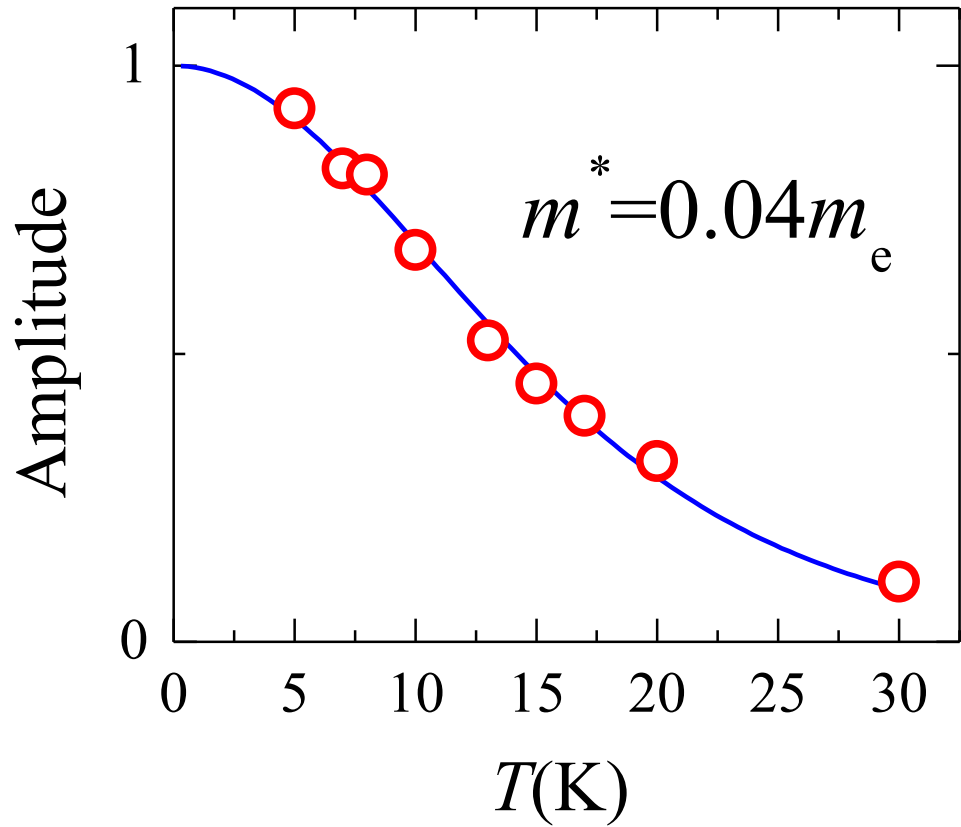


Linear dispersion: Dirac electrons

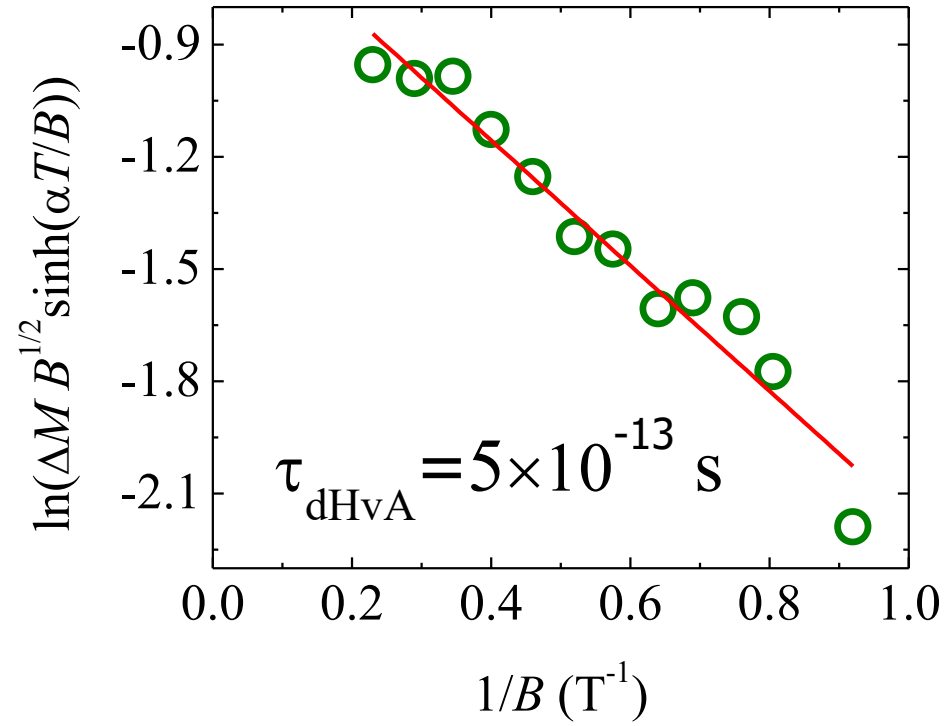
Quadratic dispersion: Schrodinger electrons



❖ Effective mass



❖ Scattering rate



Much stronger than form transport measurements

**Thank you for your
attention**