

# The in- and out-of-plane magnetisation of highly underdoped $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ single crystals

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## Background

In two recent papers [1,2] we have shown how measurements of static magnetic susceptibility  $\chi_c(T)$  of  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  single crystals for magnetic fields applied along the c-axis, and  $\chi_{ab}(T)$  for fields in the ab-plane, can give useful information about their thermodynamic properties which are still being hotly debated. SQUID magnetometry above the superconducting (s/c) transition temperature  $T_c$  is used for larger crystals, while piezolever torque magnetometry gives  $\chi_D(T) = \chi_c(T) - \chi_{ab}(T)$  for tiny crystals [2]. Here we present some new data for highly under-doped crystals with hole concentrations per  $\text{CuO}_2$  plane  $p = 0.058$  to  $0.073$ . This is the region where neutron scattering studies [3,4] give evidence for competition between incommensurate magnetic short-range order and superconductivity. We have studied crystals with three values of  $x$ , measuring  $\chi_c(T)$  and  $\chi_{ab}(T)$  immediately after fixing  $x$  by quenching on to a copper block and again after allowing sufficient time at room temperature for the Cu-O chains to order.

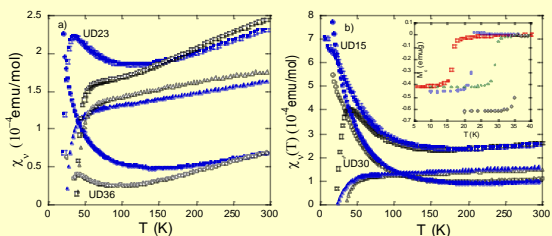


FIG. 1: (a) Temperature dependence of the static magnetic susceptibility  $\chi_c(T)$  and  $\chi_{ab}(T)$  for  $H \parallel$  the c axis and the ab plane respectively, together with the anisotropy  $\chi_c(T) - \chi_{ab}(T)$  for six  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  crystals studied in an applied magnetic field of 5 T. The inset to Fig. 1 (b) shows the superconducting transition of the  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  crystals measured on warming in 10 Gauss using a SQUID magnetometer after cooling in zero field.

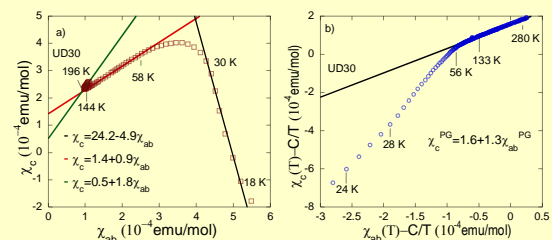


FIG. 2: (a) The static magnetic susceptibility  $\chi_c(T)$  versus  $\chi_{ab}(T)$  for  $H = 5 \text{ T}$  // the c axis and the ab plane respectively, of  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  single crystal UD30. The solid lines show linear fits. (b) The  $\chi_c(T) - C/T$  versus  $\chi_{ab}(T) - C/T$  for  $H = 5 \text{ T}$  of UD30.

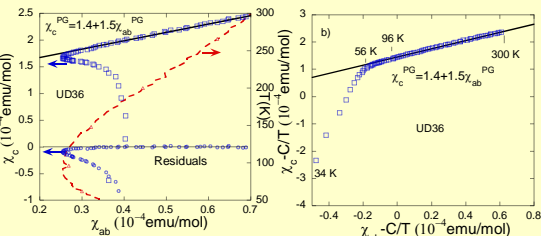


FIG. 3: (a) The static magnetic susceptibility  $\chi_c(T)$  versus  $\chi_{ab}(T)$  for  $H = 5 \text{ T}$  // the c axis and the ab plane respectively, of  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  single crystal UD36. The solid lines show linear fits. (b) The  $\chi_c(T) - C/T$  versus  $\chi_{ab}(T) - C/T$  for  $H = 5 \text{ T}$ .

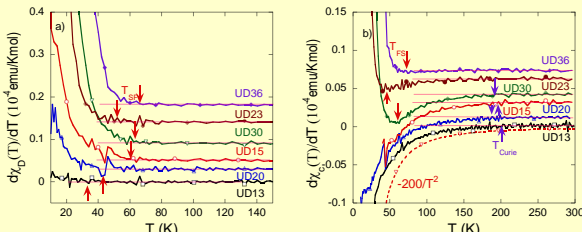


FIG. 4: (a) The temperature derivative of  $\chi_D(T) = \chi_c(T) - \chi_{ab}(T)$  at  $H = 5 \text{ T}$  for UD36, UD23, UD30, UD15, UD20 and UD13. (b) The temperature derivative of  $\chi_c(T)$  for the same crystals. For clarity the data are shifted.

## Analysis of the magnetic susceptibility data

$$\chi(T) = \chi_{PG}(T) + \chi_{FL}(T) + C/T + \chi_{VV}(T) + \chi_{core}(T) \quad (1)$$

$$\chi_{PG}(T) = N_0 \mu_B^2 \left\{ 1 - \left( \frac{E_g}{2k_B T} \right)^{-1} \ln \left[ \cosh \left( \frac{E_g}{2k_B T} \right) \right] \right\} \quad (2)$$

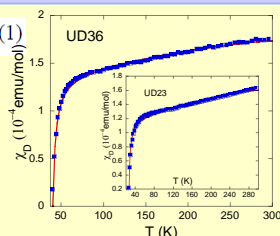
For  $T < 0.3 E_g/k_B$ , the limiting form is:

$$\chi_{PG}(T) = A \frac{2k_B T}{E_g} \ln 2$$

where  $A = N_0 \mu_B^2$ .

$$M_c^{FL}(T) = \frac{\pi k_B T H}{3\Phi_0^2} \frac{\xi_{ab}^2}{s \sqrt{1 + (2\xi_{ab}/\gamma s)^2}} \quad (3)$$

Here  $\gamma = \xi_{ab}/\xi_c$  is the anisotropy,  $\xi_{ab} = \xi_{ab}(0)/e^{1/2}$  and  $\xi_c = \xi_c(0)/e^{1/2}$ ,  $\epsilon = \ln(T/T_c)$  are the T-dependent GL coherence lengths // and  $\perp$  to the layers,  $s = 1.17 \text{ nm}$  is the distance between  $\text{CuO}_2$  bi-layers,  $\Phi_0$  is the flux quantum for pairs and  $k_B$  is Boltzmann's constant. Eq. 4 is valid when  $H < \Phi_0/(2\pi\xi_{ab}^2)$  and then the susceptibility  $\chi_c^{FL} \equiv M_c^{FL}/H$  does not vary with  $H$ . For H.L.C.  $\chi_{ab}^{FL} = 0$  in the two-dimensional (2D) limit  $s \gg \xi_c(T)$  and in the opposite 3D limit  $\chi_{ab}^{FL} = \chi_c^{FL}/g$ . The solid line shows the fit to Eq. 1 to the magnetic susceptibility data of the UD36 and UD23 crystals.



$x$	$T_c$ (K)	$10^4 C$ (emuK/mole)	$10^4 A$ (emu/mole)	$10^4 \chi_0$ (emu/mole)	$T_{PG}$ (K)	$\xi_{ab}$ (nm)	$p$ / $\text{CuO}_2$
0.42	36.2	$28.1 \pm 1$	1.49	1.52	739	3.51	0.073
0.40	30.1	$160.7 \pm 3$	1.50	1.43	770	4.22	0.069
0.42	23.3	$49.5 \pm 2$	1.86	1.34	796	4.15	0.064
0.37	20.2	$150.2 \pm 3$	1.42	1.59	802	5.28	0.063
0.40	15.7	$200.4 \pm 3$	1.45	1.45	821	6.1	0.060
0.37	13.0	$165.3 \pm 3$	1.55	1.32	833	7.51	0.058

TABLE I: Summary of results. The  $x$  values in the first column are determined from weight loss on annealing and thermogravimetric analysis in flowing argon for the present crystals. The critical temperature  $T_c$  was taken as the midpoint of the superconducting transition, as determined by measuring the field-warming magnetisation at 10 Oe after zero-field cooling.  $C$ ,  $A$ ,  $\chi_0 = \chi_{VV} + \chi_{core}$  and  $\xi_{ab}$  are the parameters of Eq. 1 of fit to the magnetic susceptibility data shown in Fig. 1. The  $T_{PG}$  is the pseudogap temperature. The values of  $p$  are obtained from Ref. 6.

## Conclusion

The main results of this work are:

- The T-dependent anisotropy well above  $T_c$  arises from the pseudogap and the g-factor anisotropy.
- At lower T, there are Gaussian s/c fluctuations.
- For all six crystals the  $\chi_D(T)$  has a weakly T-dependent linear region at higher T.
- Isotropic Curie contribution to  $\chi(T)$  with the onset temperature below 200 K.
- Ordering the CuO chains reduces the Curie contribution to  $\chi(T)$

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## References

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Hrvatska zaklada za znanost